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EHB322E Digital Electronic Circuits
MIDTERM II

Duration: 120 Minutes

Grading: 1) 60%, 2) 40%

Exam is in closed-notes and closed-books format; calculators are allowed.

For your answers please use the space provided in the exam sheet

GOOD LUCK!

$$x_4^9 x_5$$

- 1) Consider a Boolean function $f = gx_2x_3 + \overline{x_1}\overline{x_2} + x_1\overline{x_3}$ where $g = x_4 + x_5$. Suppose that all NMOS transistors are identical and all PMOS transistors are identical. $V_{DD}=5V$ and $|V_{TH}|=1V$ (Both for NMOS and PMOS).
Equivalent resistor for an NMOS transistor: $R_N=12k\Omega$
Equivalent resistor for a PMOS transistor: $R_P=24k\Omega$
 Suppose that the output circuit node has a capacitance value of $10pF$. Neglect internal and other node capacitors.

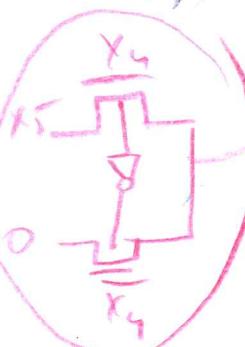
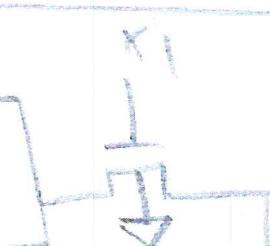
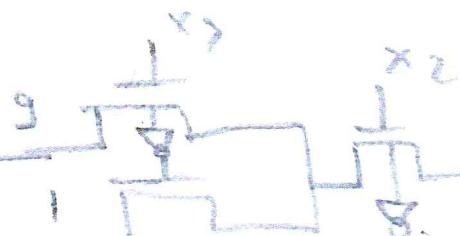
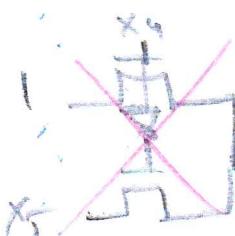
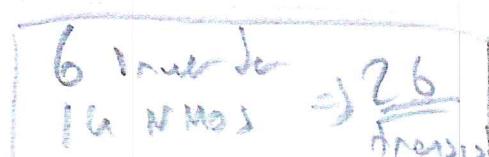
Implement f with “NMOS Pass Transistor Logic – PTL - Network(s)” and “CMOS Inverters” with minimum number of transistors such that there is no threshold voltage drop at the output (output is VDD or GND all the time). For the PTL networks use the ordering of $x_1 - x_2 - x_3 - x_4 - x_5$. Also use only variables $x_1 - x_2 - x_3 - x_4 - x_5$ as inputs, not their negated forms. Find the **minimum number** of transistors needed. Find the **worst case (largest) t_{PLH}** and **t_{PHL}** values (total of 2 values).

$$g = x_4(1) + \bar{x}_4(x_5)$$

$$A_{106} = x_1(x_2x_3g + \bar{x}_3) + \bar{x}_1(x_2x_3g + \bar{x}_3) = x_1(x_2(x_3g + \bar{x}_3) + \bar{x}_2(\bar{x}_3)) +$$

$$= x_1 \left(x_2 (x_3(g) + \bar{x}_3(1)) + \bar{x}_2 (x_3(g) + \bar{x}_3(1)) \right) - \bar{x}_1 \left(x_2 (x_3(g) + \bar{x}_3(1)) \right)$$

$$+ \bar{x}_1(x_2(9) + \bar{x}_2(0)) + \bar{x}_2(1)$$



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15

$$t_{PAE} = t_{PAH} \approx 0,63 (4,12 \cdot 10^{10} \text{pp}) = \underline{\underline{331,2}} \text{ ns}$$

165, S₁₅

$$g = x_4 + x_5$$

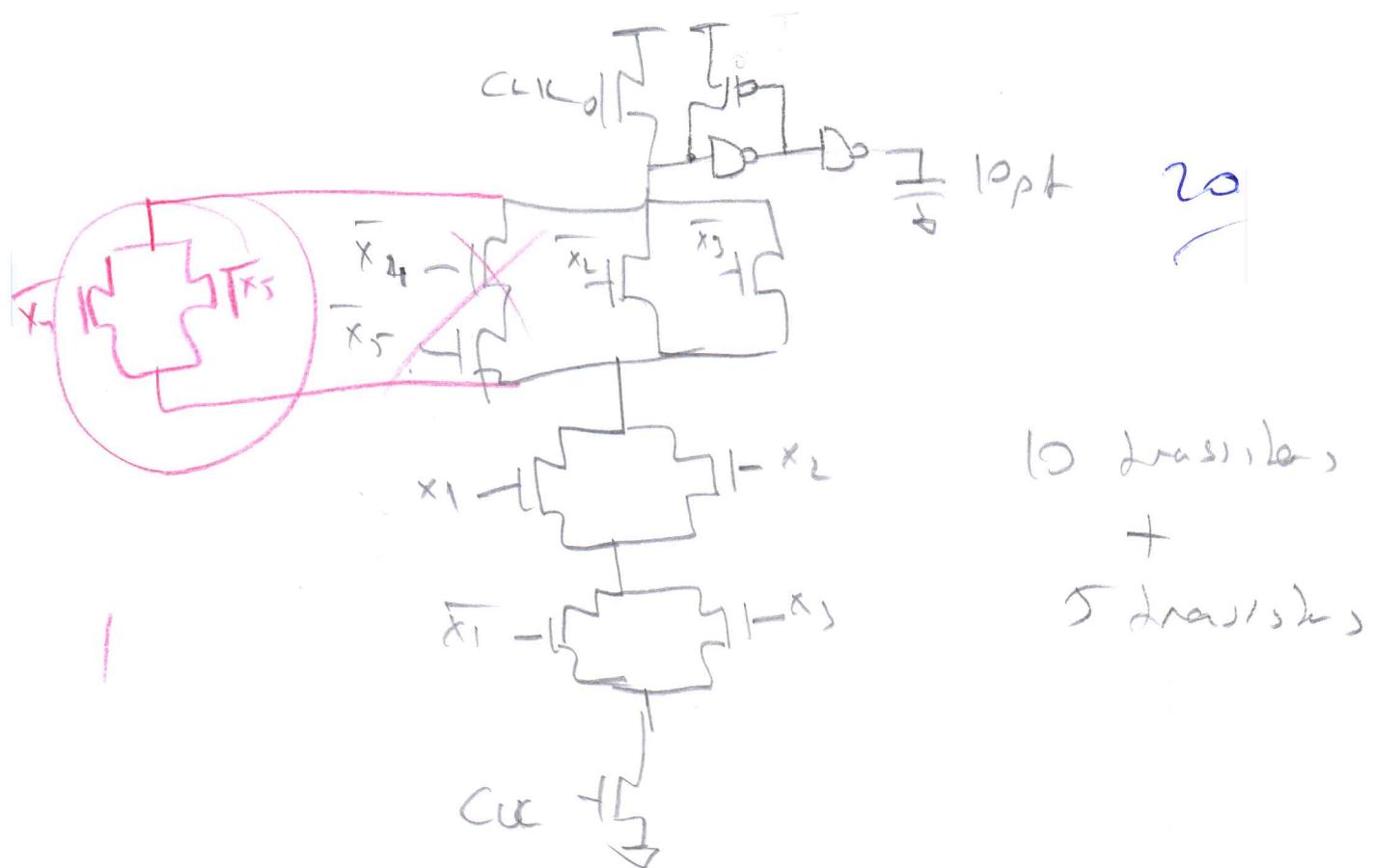
- 2) Consider a Boolean function $f = gx_2x_3 + \bar{x}_1\bar{x}_2 + x_1\bar{x}_3$ where $g = x_4 + x_5$. Implement f with "Dynamic Logic" using "a Pull-Down NMOS Network" using minimum number of transistors such that there is no charge sharing problem. Find the **minimum number** of transistors needed.

Equivalent resistor for an NMOS transistor: $R_N = 12\text{k}\Omega$

Equivalent resistor for a PMOS transistor: $R_P = 24\text{k}\Omega$

Suppose that the output circuit node has a capacitance value of 10pF . Neglect internal and other node capacitors. You can use variables $x_1 - x_2 - x_3 - x_4 - x_5$ and their negations as inputs. Find the **worst case (largest) t_{PHL} and t_{PLH} values** (total of 2 values).

$$f = x_2x_3(x_4+x_5) + \bar{x}_1\bar{x}_2 + x_1\bar{x}_3$$



$$\text{wc } t_{PHL} = 0,69 \cdot 5(12k) \cdot 10_p = 416\text{ns} \quad (6)$$

$$\text{wc } t_{PLH} = 0,69 \cdot 24k \cdot 10_p = 165,6\text{ns} \quad (6)$$

$\text{wc } t_{PHL} = 0,69 (4 \times 6k) \cdot 10_p = 165,6\text{ns}$
$\text{wc } t_{PLH} = 0,69 \cdot 12k \cdot 10_p = 82,8\text{ns}$